TRStalker: an Efficient Heuristic for Finding Fuzzy Tandem Repeats

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ABSTRACT

Motivation: Genomes in higher eucaryotic organisms contain a substantial amount of repeated sequences. Tandem Repeats (TRs) constitute a large class of repetitive sequences that are originated via phenomena such as replication slippage and are characterized by close spatial contiguity. They play an important role in several molecular regulatory mechanisms, and also in several diseases (e.g. in the group of trinucleotide repeat disorders). While for tandem repeats with a low or medium level of divergence the current methods are rather effective, the problem of detecting TRs with higher divergence (fuzzy TRs) is still open. The detection of fuzzy TRs is propaedeutic to enriching our view of their role in regulatory mechanisms and diseases. Fuzzy TRs are also important as tools to shed light on the evolutionary history of the genome, where higher divergence correlates with more remote duplication events.

Results: We have developed an algorithm (christened TRStalker) with the aim of detecting efficiently Tandem Repeats that are hard to detect because of their inherent fuzziness, due to high levels of base substitutions, insertions and deletions. To attain this goal we developed heuristics to solve a Steiner version of the problem for which the fuzziness is measured with respect to a motif string not necessarily present in the input string. This problem is akin to the “generalized median string” that is known to be an NP-hard problem. Experiments with both synthetic and biological sequences demonstrate that our method performs better than current state of the art in order to extend our comprehension of the role of TRs in biological mechanisms. Existing ab initio detection of repetitive elements that are not based on prior knowledge accumulated in data bases, are still important in order to extend our comprehension of the role of TRs in biological mechanisms. Existing ab initio tools are successful when the TR exhibits a moderate amount of divergence and when the TR is easily validated. However, there is an emerging need for new tools that are able to cope with higher levels of sequence divergence and/or TR computational more difficult to validate. For example, Boeva et al. (Boeva et al., 2006) study so called Fuzzy Tandem Repeats and their role in gene expression. The technique in (Boeva et al., 2006) works well for the Hamming metric (only substitutions and no insertions/deletions allowed) and for short repeat units (from 3 to 24 bp) that are common in micro- and mini-satellite families.

Some of the most successful ab initio tools, such as TRF (Benson, 1999) and ATRHunter (Wexler et al., 2005), are based on a multi-stage filtering approach (see also (Peterlongo et al., 2009)). In the first stage the input sequence is analyzed to detect, via statistical criteria, likely position and length of candidate subsequences. The final stage is the validation one in which a more expensive test is applied to candidate substrings passing the first stages, so to determine an output that matches the implicit definition of TR and the user-defined filtering parameters.

1 INTRODUCTION

Tandem Repeats (TRs) are multiple (two or more) duplications of substrings in the DNA that occur contiguously, and may involve some base mutations (such as substitutions, insertions, and deletions). Tandem Repeats of several forms (satellites, microsatellites, minisatellites, and others) have been studied extensively because of their role in several biological processes. In fact, TRs are privileged targets in activities such as fingerprinting or tracing the evolution of populations (Kelkar et al., 2008; Vogler et al., 2006). Several diseases, disorders and addictive behaviors are linked to specific TR loci (Wooster et al., 1994). The role of TRs has been studied also within coding regions (O’Dushlaine et al., 2005) and in relation to gene functions (Legendre et al., 2007). Large scale comparative studies on TRs of the human genome are described in (Ames et al., 2008; Warburton et al., 2008). Data Bases of repetitive elements such as RepBase (Jurka et al., 2005) and TRDB (Gelfand et al., 2007) are now available; and the detection of repetitive elements via library-based similarity matching, for example by using the tool Repeatmasker (Smit et al., 2004), is a popular practice. However, tools for ab initio detection of repetitive elements that are not based on prior knowledge accumulated in data bases, are still important.

1.1 Our Contribution

Our contribution is a novel multi-stage filtering algorithm, called TRStalker, for finding long fuzzy tandem repeats under the edit distance, that introduces new techniques (w.r.t. previous TR finding algorithms) in all stages. For the first stage, where over-represented distances between probes are sought, we employ gapped q-grams (Burkhardt and Kärkkäinen, 2003) in place of the standard ungapped q-grams in order to collect evidence on the candidate substrings. Gapped q-grams have been used before in the context of textual and biological database searching, but less so in the area of

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tandem repeats detection (with the exception of the system TEIRESIAS (Stolovitzky et al., 1999)). Because of errors due to insertion/deletions the period of a TR is subject to fluctuations, thus we employ a weighting scheme with exponential decay so to reinforce the signal even in presence of this smearing effect. Finally we use ranking instead of thresholds when deciding the substrings to pass to the next phases, in order to concentrate the computational effort on the zones with candidates with higher weight. For the final validation stage we employ an NP-complete definition of TR involving the concept of generalized median string under edit distance (de la Higuera and Casacuberta, 2000; Sim and Park, 2003), together with an efficient heuristic for computing an approximation of such median string (Jiang et al., 2003) previously not used in a biological context.

By extensive experimental comparisons of TRStalker with two state-of-the-art tools, namely TRF and ATRHunter, we did find out that TRStalker has consistently better performance for a large range of error and length parameters for the class of fuzzy Tandem Repeats under edit distance, with a recall ranging from 100% to 60%. Thus TRStalker improves the capability of TR detection for classes of TRs for which existing methods do not perform well. Tests performed on standard evolutionary TRs definitions (verifiable in polynomial time) also show recall performance close to 100%. Incidentally, this result confirms of the power of the new techniques developed for the initial filtering phase.

1.2 State of the Art

We will briefly survey the state of the art in finding tandem repeats. First we will describe methods that for a given definition of TR are able to find all maximal substrings in the input that match the definition (exhaustive algorithms). Often exhaustive algorithms may not be available, or when available they may be too slow in practice. Thus, several heuristic algorithms have been developed which are shown experimentally to be able to detect a large fraction of TRs efficiently. Note that the time/precision trade-off is severely influenced by the allowed error thresholds. Performance often degrades quickly with increasing error levels.

Exhaustive algorithms. When we allow no error, it is possible to find all maximal exact TRs in a string of length \(n\) in time \(O(n)\) (Kolpakov and Kucherov, 1999; Gusfield and Stoye, 2004). When we allow two consecutive repeats to differ by an amount at most \(k\) (either in Hamming or in edit distance) Landau, Schmidt and Sokol (Landau et al., 2001) give exhaustive algorithms running in time \(O(nk \log(n/k))\) for Hamming distance, and \(O(nk \log k \log(n/k))\) for edit distance. A simpler algorithm with the same asymptotic complexity for the edit distance is proposed by Sokol, Benson and Tojeira (Sokol et al., 2007). Kolpakov and Kucherov (Kolpakov and Kucherov, 2003) improved the bound for the Hamming distance to \(O(nk \log k + s)\) where \(s\) is the number of TRs found. For the Hamming distance, Krishnan and Tang (Krishnan and Tang, 2004) give an exhaustive method running sequentially in time \(O(n^3)\), that can be easily implemented onto a parallel architecture, since every possible pattern length is searched independently.

Heuristic algorithms. The algorithmic techniques in (Kolpakov and Kucherov, 1999, 2003) have been extended in the tool mcreps (Kolpakov et al., 2003) so to be able to handle approximate TRs under edit distance, with some additional heuristic filtering steps.

The tool TRF (Tandem Repeat Finder) developed by Benson (Benson, 1998, 1999), based on statistical filtering of zones of DNA likely to contain TRs, is currently one of the standard heuristic methods. ATRHunter (Wexler et al., 2004) by Wexler et al. is also based on a statistical filtering approach, placing greater emphasis in techniques for designing thresholds for the quantities of interest. Other proposed heuristics for finding TRs are REPuter (Kurtz and Schleiermacher, 1999; Kurtz et al., 2001), STRING (Parisi et al., 2003), TEIRESIAS (Stolovitzky et al., 1999), TandemSWAN (Boeva et al., 2006). A class of papers (see e.g. (Sharma et al., 2004), (Brodzik, 2007), (Buchner and Janjarasjitt, 2003), (Gupta et al., 2007)) tackle the problem of finding tandem repeats as a problem in signal processing theory and usually map the input string into a time-signal in a suitable numerical domain for which several spectral techniques can be used, such as the Periodicity Transform or the Fourier Transform. Other methods use data compression techniques to detect repetitive elements (Rivals et al., 1997).

The methods cited above are rather general since they aim at treating efficiently TRs in a wide range of length values. There is also a large class of methods that are aimed at handling particular or special classes of TRs such as: microsatellites (e.g. IMEx (Mudunuri and Nagarajaram, 2007)), palindromic repeats (e.g. CRISPFinder (Grissa et al., 2007)), Variable Length Tandem Repeats (VLTR) and Multi-period Tandem Repeats (MPTR) (Hauth and Joseph, 2002), Variable Number Tandem Repeats (VNTR) (Sammeth and Stoye, 2006). Since the focus of our research on TRs at present is on the more classical forms of TRs we do not dwell longer on them. However, we just note that often methods for MPTR, VNTR, VLTR use standard TR finding as a subroutine, thus our proposed algorithm can increase also the ability to detect such higher order structures.

Systematic comparison among TR finding tools and algorithms operating “ab initio”, that is without support of specific biological data bases has been tackled in recent years (Leclercq et al., 2007; Saha et al., 2008). A survey of problems on Tandem Repeats in the context of evolutionary mechanisms, such as the construction of TR Evolutionary Trees, is proposed in (Rivals, 2004) (see also (Elemento and Gascuel, 2002)).

1.3 Organization of the paper

The paper is organized as follows: in Section 2 we describe at a high level the principles guiding the different phases of the TRStalker algorithm. Section 3 gives a more technical description of key ingredients of TRStalker and discusses the formal definition of fuzzy TR employed. Section 4 describes the experiments devised to demonstrate the capacity of TRStalker in detecting fuzzy TRs, and a few interesting fuzzy TRs found in sequences of biological significance.

2 APPROACH

An example. To focus on the main ideas, let us consider the very simple case of Exact TR. Consider an alphabet \(\Sigma = \{A, C, G, T\}\) of four symbols, and a string \(X = x_1, x_2, \ldots, x_t\) formed by the concatenation of \(t\) strings \(x_i\), embedded in a random string \(Y\), where \(x_i = x_j\) for all \(i\) and \(|x_i| = k\); thus all replicas of \(x_1\) are of the same length. An ungapped \(q\)-gram is a string of \(q\) symbols from \(\Sigma\) that appears as a consecutive sequence of \(q\) symbols in \(Y\). We aim at discovering \(k\) just by looking at the distances between occurrences of homologous (i.e. identical) \(q\)-grams in \(Y\).
period $k$ will appear at least $(k - q + 1)(t - 1)$ times as the distance between homologous probes. More generally the distance $hk$, an integer multiple of $k$, will appear at least $(k - q + 1)(t - h)$ times for each value $h = 1, \ldots, t - 1$. A gapped $q$-gram is a sequence of $q$ characters from $\Sigma$ with additional “don’t care” symbols, also called “gaps”, that appears as a consecutive sequence in $Y$. For gapped $q$-grams similar formulae hold. For values of $k$ and $t$ large enough, the period $k$ and its integer multiples will occur more frequently than the expected number of occurrences of any distance of homologous $q$-grams in a random string, thus the empirical number of occurrences of the value $k$ and its multiples will tend to be in the higher part of a ranking by frequency. This observation holds true as long as the length of the super-string $Y$ is sufficiently limited so that the frequencies generated by the random portion of $Y$ do not overrun the frequencies generated by $X$. An exact characterization of such a distribution in terms of the parameters $k$, $q$ and $|Y|$ is complex since it can be characterized as the sum of non-independent random variables each with a negative binomial distribution. However we avoid the issue of characterizing exactly such a distribution by: (1) splitting the input string into blocks of predefined length and limiting the analysis to each block separately, providing mechanisms to deal with TRs stranded across the block boundaries; (2) ranking the periods by weighted frequency and exploring only the top $L$ positions (for $L = 50$ in our experiments). Note that in most cases the top ranking periods not corresponding to tandem repeats will be discarded quickly when the positional density is considered, thus we can deal with TRs stranded across the block boundaries; (2) ranking the periods by weighted frequency and exploring only the top $L$ positions (for $L = 50$ in our experiments). Note that in most cases the top ranking periods not corresponding to tandem repeats will be discarded quickly when the positional density is considered, thus we can deal with TRs stranded across the block boundaries.

**Positional density**. We further exploit the property of TRs that the same period is detected by probes in near-by positions. We define a notion of positional $k$-density, that is the density of probes that contribute to the counter for the candidate period $k$. We search for positions in $Y$ of high $k$-density as candidates for the starting point of a TR.

**Validation**. In the third phase we take each candidate pair $(p, i)$ and we test explicitly whether there is a tandem repeat of period $p$ starting in position $i$ according to the definition (see section 3). In particular when using the definition of a Steiner-STR (see subsection 3.2) we use a double filtering. The first filter uses a wraparound dynamic programming technique (WDP) (Fischetti et al., 1993). The second filter computes an approximation to the generalized media string (inspired by an algorithm proposed in (Jiang et al., 2003)). In this phase, besides validating the TRs, we discover the (fractional) repetition number of the TRs eventually extracted.

**Postprocessing**. As a post processing we check for inclusion the TRs found and we filter out those TRs completely enclosed in another one. For TRs in the same position and length but different period we report the TR with shorter period. Finally we align the approximate generalized median string with the TR units so to give a graphical compact output of the TR. 

### 3 METHODS

#### 3.1 Basic Definitions

A Tandem Repeat in a DNA sequence is the repetition of two or more contiguous exact or approximate copies of a substring (called the motif) of the tandem repeat. 

**Exact TR**. Formally, given an alphabet $\Sigma$, and a set of strings $x_i \in \Sigma^*$, consider the concatenation $X = x_1 x_2 \ldots x_i$. The (string) $X$ is an exact tandem repeat (ETR) of period $k$ and repeat number $t$, when $|x_i| = k$ and $x_i = x_1$, for each $i \in [1, \ldots t]$. In general we may suppose there is a longer string $Y$ of which $X$ is a substring. The string $x_1$ that is repeated exactly is called the motif of the ETR. A TR $X$ is called maximal if it cannot be extended in $Y$ while still being a TR.

**Approximate TR (ATR)**. Exact tandem repeats are sometimes found in biological sequences, but they tell us only part of the story, thus several notions of an approximate tandem repeat have been developed. Denote with $D_H(a, b)$ the hamming distance of two strings with equal length. If the length of $a$ and $b$ is different we consider the smallest possible mismatch in an alignment of the two strings without gaps. Denote with $D_E(a, b)$ the edit distance of the two strings $a$ and $b$. 

The candidate periods are then sorted by the weight $w_3(\cdot)$, and processed in decreasing order.

#### 3.2 Preprocessing

**Anti-smear weighting**. If $q_1$ and $q_2$ are occurrences of homologous $q$-grams in $X$ at distance $k$, before the implant of mutations, the effect of insertion and deletions on the positions of the string $X$ between $q_1$ and $q_2$ is to alter their distance so that a different period $k'$ is detected. The difference $k - k'$ is equal to the algebraic sum of number of insertions and deletions in the positions between $q_1$ and $q_2$. Assuming that such any position can be an insertion or a deletion independently with the same probability, the random variable $k - k'$ is distributed as a sum of independent r.v. with values in $\{-1, 0, 1\}$ with mean value 0, thus, by a Chernoff bound argument, its tail distribution decays exponentially (Motwani and Raghavan, 1995; Mulmuley, 1993). Also near-by probes in $X$ have small variations in the value of the shift $k - k'$. Inspired by the above observation we devise a weighting scheme that increments the total weight of period $k$ if another period of value $k$ is discovered in a near-by position, with weights that decay exponentially with $|k - k'|$. The final weight $w_0(k)$ for a given period $k$ is the sum of the individual anti-smear weights computed above for probes at distance $k$.

**Multiplicity weighting**. Let $w_0(k)$ be the weight of the period $k$ as assigned by the anti-smear weighting procedure. As observed before for a TR with a large number of copies we will find also integer multiples of $k$ with a relatively high frequency. We take advantage of this fact and compute new weights:

$$w_1(k) = \sum_{h \geq 1} w_0(hk).$$

The candidate periods are then sorted by the weight $w_1(\cdot)$, and processed in decreasing order.
3.2 Our definitions of TR

We used two different definitions of TRs:

- Neighboring TR (NTR): a string X, so that for each i ∈ [1, .., t−1], \( D_E(x_i, x_{i+1}) \leq \mu |x_i| \), for a user defined parameter 0 ≤ \( \mu \) ≤ 1.
- Steiner-STR with sum: a string X = x_1x_2..x_t for which two conditions hold for a user defined error parameter 0 ≤ \( \mu \) ≤ 1, and constant c with 1 ≤ c ≤ 2:
  (a) for each i ∈ [1, .., t−1], \( D_E(x_i, x_{i+1}) \leq c|x_i| \),
  (b) there exists a Steiner string \( \tilde{x} \in X^* \) so that
  \[
  \sum_{i \in [1..t]} D_E(x_i, \tilde{x}_i) \leq \mu |X|.
  \]

Intuitively, in a Steiner-TR the TR consists of \( t \) duplications of a single Steiner consensus string \( \tilde{x} \) with \( \mu |x| \) mutations on average in each copy, such that consecutive copies do not diverge too much w.r.t. the average. Note that condition (a) is vacuous for \( \mu \geq 1/c \). The choice for the constant \( c \) depends also on the level of divergence. For low divergence \( c = 2 \) is a sensible choice since two copies at distance \( \mu |x| \) from \( x \) are also at distance at most \( 2\mu |x| \) from each other by the triangular inequality. Thus (a) is a necessary condition for (b). For higher level of divergence above 30%, the value \( c = 2 \) is too loose and we use a lower value \( c = 1.5 \), so to maintain a good filtering ability of condition (a) and to avoid having as a possible solution a TR where the consecutive pairs may have a very irregular divergence.

3.3 Output of TRStalker

The aim of TRStalker is to produce a ranked list of all maximal tandem repeat sub-sequences present in the input string that satisfy the definition above (Neighboring-TR or Steiner-STR), where maximality means that it is not possible to extend the TR (as a substring of the input) to the left or to the right without violating the definition within the given user defined parameters. We avoid producing meaningless TRs by imposing also a lower bound on the TRs length.

3.4 Other definitions

In (Sokol et al., 2007) it is used the following definition: \( X \) is called a k-edit Approximate Tandem Repeat when \( \sum_{i=1}^{t-1} D_E(x_i, x_{i+1}) \leq k \), where the last repeat \( x_t \) might be incomplete so \( D_E(x_1, x_2) \) is computed as the minimum edit distance of \( x_1 \) and the prefixes of \( x_{1..t−1} \). This definition is inspired by the evolutionary model of TRs in which it is assumed TRs are generated by duplicating the last copy of a previous TR, possibly with duplication errors that truncate it. A k-edit repeat is maximal if it cannot be extended either to the left or to the right without violating its definition.

In (Wexler et al., 2004) for a similarity function \( \phi \) that measures the alignment score of two sequences, it is defined a \( \eta \)-Simple Approximate Tandem Repeat (\( \eta \)-SATR) a string \( X = x_1..x_t \) such that: there exists a motif \( \tilde{x} \in X^* \) so that for every \( i \in [1..t] \), \( \phi(x_i, \tilde{x}_i) \geq \eta \). In other words the TR consists of \( t \) duplications of a single consensus string \( \tilde{x} \) with mutations. Such string \( \tilde{x} \) is also called a Steiner motif if \( \tilde{x} \) is not constrained to be equal to some repeat \( x_i \). Often in practice \( \tilde{x} \) is chosen as the repeat \( x_i \) that minimizes the error function, and is called a pivot motif. The distinction is critical since, as mentioned before, Steiner motifs lead to NP-complete recognition problems, while pivot motifs do not.

The \( \eta \)-Neighboring Approximate Tandem Repeat (\( \eta \)-NATR) is a string \( X \), so that for each \( i \in [1, .., t−1] \), \( \phi(x_i, x_{i+1}) \geq \eta \) (Wexler et al., 2004). The Pairwise Approximate Tandem Repeat (PATR) is a string \( X \), such that for every pair of indices \( i, j \in [1, .., t] \) with \( i \neq j \) we have \( \phi(x_i, x_j) \geq \eta_{ij} \), where \( \eta_{ij} \) is set to be a monotonically decreasing function of \( |i−j| \), thus allowing more slackness when comparing distant copies of the basic motif.

In (Krishnan and Tang, 2004) it is used a definition similar to that of the Neighboring Approximate Tandem Repeat, except that the Hamming distance is used and that the threshold is not absolute but relative to the length. A \( \gamma \)-Hamming Approximate Tandem Repeat (\( \gamma \)-HATR) is a string \( X \) such that: for each \( i \in [1, .., t−1] \), \( D_H(x_i, x_{i+1}) \leq 2|x_i|\gamma \).

In (Stolovitzky et al., 1999) a more complex definition is given that takes into account the substring alignment score density function for pairs of random substrings of a given length. Here the definition of a TR \( X \) depends on the properties of the longer string \( Y \) into which \( X \) is embedded. In particular a \((\mu, p)\)-TR must comply to two conditions: 1) \( \sum_{i=0}^{t} \phi(x_i, x_{i+1}) \geq (t−1)\mu \), that imposes an average high similarity score for adjacent repeats, and 2) define \( \alpha(p, k) \) as the value of similarity such that there is probability \( p \) that two random substrings of length \( k \) in \( Y \) have similarity above \( \alpha(p, k) \).

There must be an index \( q \in [1, .., t] \) such that \( \phi(x_q, x_{q+1}) \geq \alpha(p, k) \) for all \( j \in [1, .., t] \). Note that this condition limits the dispersion of the similarity with respect to one of the copies (called the pivot).

TRF (Benson, 1999) uses as final validation algorithm the wraparound dynamic programming technique (WDTP) that tests efficiently the alignments of a given candidate motif with the surrounding portions of the input sequence, so to determine the maximum number of adjacent repetitions within a user-defined score bound. This implies a notion of TR akin to that of simple approximate tandem repeats (SATR) with pivot motif. Classical results on string alignments (Gusfield, 1997, page 351) ensures that, for the metric score given by the sum of motif-repeats distances, the solution found using the optimal pivot motif has a score within a factor \((2 − 1/\epsilon)\) of the score induced by the optimal Steiner Motif. For low levels of errors one could use a pivot-SATR definition doubling the error threshold to capture a Steiner-SATR, however for higher error levels (say, above 25%), doubling the error threshold forces the existing systems to work in a range of values (say, above 50%) where most methods do not perform well.

3.5 Gapped q-grams

Let \( I \) be a finite subset of non-negative integers. We call \( I \) an index set. The span of \( I \) is \( \text{span}(I) = \max(i−j) \mid i, j \in I \), the position of \( I \) is \( \text{pos}(I) = \min(i) \mid i \in I \), and the shape of \( I \) is \( \text{shape}(I) = (\{ i−\text{pos}(I) \mid i \in I \}) \). When set \( I \) has \( |I| = q \) and \( \text{span}(I) = s \), its shape belongs to the class of \((q,s)\)-shapes. Any set of non-negative integers \( Q \) containing 0 is a shape. For an alphabet \( \Sigma = \{ A, C, G, T \} \), a string \( S \in \Sigma^* \) of length \( n \) can be seen as a function defined over \([0, n−1]\) with values in \( \Sigma \), and for any subset \( I \subset [0, n−1] \) the restriction of \( S \) to \( I \), denoted by \( S[I] \) is a substring of \( S \).

Given any shape \( Q \) in the class of \((q,s)\)-shapes, all sets \( I \subset \{ 0, .., n−1 \} \) such that \( \text{shape}(I) = Q \), form the set of \( \text{Indexes}(Q,n) \). We can use elements from the \( \text{Indexes}(Q,n) \) to generate restrictions for the string \( S \). Given two index sets \( I_1, I_2 \in \text{Indexes}(Q,n) \), we call them matching (or homologous in \( S \), if \( S[I_1] = S[I_2] \)). The value \( \text{pos}(I_1)−\text{pos}(I_2) \) is called the period of the match.

An index set \( I \) with \( |I| = q \) and \( \text{span}(I) = q − 1 \) is called an ungapped q-gram since its shape is \( \text{shape}(I) = \{ 0, q−1 \} \). If we have an index set \( J \) with \( |J| = q \) and \( \text{span}(J) = s \geq q \) we have a gapped q-gram since its shape is formed of non consecutive integers. In order to generate a population of candidate periods we consider now all possible \((q,s)\)-shapes with \( q = 3 \) and \( s = 4, 3, 2 \). Denoting with \( − \) the gaps and with \# symbols from \( \Sigma \), (the first and last positions must be always \#), we have the \((3,3)\)-shapes \( \#\# − \#\# − \#\# − \#\# \), and \((3,2)\)-shapes \#\# − \#\# and \((3,2)\)-shape \#\#.

As noted in (Burkhardt and Kärkkäinen, 2002) and (Burkhardt and Kärkkäinen, 2002), if we fix an ungapped shape and an error level in Hamming distance, there are error patterns for which every corresponding ungapped q-gram is affected by error. In contrast, with the same Hamming error level, for some gapped shapes, there are always some gapped q-grams unaffected by the injected error. Thus using a small complete family of gapped q-grams we can detect the correct period in situations where ungapped q-grams cannot.\(^1\)

\(^1\) A precise characterization of the relative gain under different error models would be theoretically interesting but is now beyond the focus of this paper.
3.6 Anti-smear weighting

Let \( P \) be a \( q \)-gram in the input string \( Y \) at position \( i \). Let \( j_1, \ldots, j_h \) be the next \( h \) occurrences of \( P \) in \( Y \) following the occurrence at position \( i \). The corresponding detected distances are \( d_{ij} = j_g - i \), for \( g \in \{1, \ldots, h\} \). For the period \( x_g \), we increment its weight:

\[
 w_d(x_g) = w_o(x_g) + 1 + \sum_{y \in Q} 2^{-|x_g - y|},
\]

where \( Q \) is a queue holding the last \( H \) detected distances in the sequential scan of the input string \( Y \). After the weight update, we enqueue all \( h \) values \( x_g \) in the queue \( Q \), and we dequeue an equal number of \( h \) items. In line with other constants fixed in TRStalker, we have chosen \( h = 5 \) and \( H = 20 \) since they do work well in our synthetic experiments for a large range of TR error and length values. A fine tuning of these parameters as a function of the characteristics of the TR sought is possible, but beyond the focus of this paper.

3.7 Positional Density

Let \( k \) be the period under investigation. Consider the set \( K_k \) of the positions of those \( q \)-grams (i.e. substrings of \( Y \)) that contribute to the weighting of \( k \) through the multiplicity weighting. In order to avoid double counting we always take the position of the first of the two matching probes. Note that, if a position is shared by several pairs of probes it will be counted only once. Let \( f : \{1, \ldots, |Y|\} \rightarrow \{0, 1\} \) the characteristic function that for each position in \( Y \) denote the membership of that position to \( K_k \). Consider the \( k \)-window smoothing of \( f \): \( F(i) = \sum_{j=1}^{k} f(j) \) that computes the \( k \)-smoothed density of the function \( f \), for \( i \in \{1, \ldots, |Y| - k\} \). Finally we define a threshold \( t(k) \) proportional to the average \( k \)-density by a user-defined constant, and we consider as a candidate position set \( CP(Y, k) = \{i \in \{1, \ldots, |Y| - k\} | F(i) \geq t(k)\} \). The output of this positional density computation is a sequence of pairs \((k, i)\) where \( k \) is a candidate period and \( i \) a candidate position.

3.8 Validation

The definition of Steiner-STR is composed of two conditions that will be tested in cascade starting from the one less computationally demanding.

Testing condition (a). The wraparound dynamic programming technique in (Fischetti et al., 1993) solves the following problem. Given a string \( P \) of length \( n \) and a text \( T \) of length \( n \), with \( n \ll n \), find the best alignment of \( P^n \) (concatenation of \( n \) copies of \( P \)) in \( T \), in time and storage \( O(nm) \). Note that a naive application of the standard dynamic programming based optimal alignment of two strings would require \( O(n^2 m) \) time/storage. We modify the WDP approach in order to (1) work with edit distance instead of similarity matrices (2) take as parameter the candidate initial tandem copy in positions \([i, i + k - 1]\) and as text an adjacent portion of the input string \( |O(m)| \). (3) we iteratively expand the text length till the termination condition is met. (4) we stop the matching as soon as the next adjacent copy of the TR differ from the previous one by more than \( \epsilon m \) in edit distance.

Testing condition (b). Let \( x_1, \ldots, x_t \) be the candidate TR to test for property \( (b) \) that passed the test for property \( (a) \). We incrementally compute an approximate generalized median \( x_\hat{a} \), using \( x_i \) and the previously computed approximate generalized median \( x_{\hat{a} - 1} \). Initially \( x_1 = x_1 \). Let \( k \) and \( h \) be two positive integers and \( K = \{j/k| j \in [0, k]\} \) be the set formed by \( k + 1 \) equally spaced real values between 0 and 1. For each value \( \alpha \in K \) we determine up to \( h \) medium strings between \( x_i \) and \( x_{\hat{a} - 1} \) with weight \( \alpha \). This set of at most \( h k \) candidate strings is then searched for the string \( \hat{a} \) that minimizes the function \( \sum_{j=1}^{h} D_e (a, x_j) \). So we set \( x_\hat{a} = a \) and start the next iteration.

Selecting larger values of \( q \) and \( s \), as a function of the period to be detected and the error level, may increase the filtering ability of the method at the cost of slower computations. Exploring these connections is left for future research.

A medium string of weight \( \alpha \in [0, \ldots, 1] \) of two strings \( a \) and \( b \) is obtained as follows. Compute the edit distance \( \epsilon = D_e(a, b) \) and record the set \( \{a, b\} \) of edit operations that transform \( a \) into \( b \). Pick any subset of \( \{x_\alpha\} \) in \( \{a, b\} \). The median weighted string \( c \) is obtained by applying those operations to the string \( a \). It is not difficult to show that it holds that \( D_e(a, c) = \alpha D_e(a, b) \) and \( D_e(b, c) = (1 - \alpha) D_e(a, b) \). Note that, depending on the value of \( \epsilon \) we have \( \{x_\alpha\} \) different subsets of \( \{a, b\} \) we can choose. In our algorithm we randomly select \( min(h, |\{\alpha\}|) \) of them.

3.9 Evaluation of recall in synthetic sequences

In order to measure the quality of the TRs reported by TRStalker and by other benchmark algorithms in our synthetic experiments we need to give a score to a pair of TRs. The higher the similarity of the two TRs, the higher should be the score. Since perfect equality is rare we need a more flexible score function. A TR can be characterized by the triple \((b, p, r)\), where \( b \) is the initial position, \( p \) the period, \( r \) the repetition number. Also, the same TR covers the positions in \( Y \) from index \( b \) to \( b + rp - 1 \). We identify the TR with the set of positions \( \{b, b + rp, \ldots, b + rp - 1\} \). Given two tandem repeats \( TR_1 \) and \( TR_2 \) represented as sets of positions, the classical Jaccard coefficient measure of set similarity \( J_C \) is:

\[
 J_C(\overline{T R_1}, \overline{T R_2}) = \frac{|\overline{T R_1} \cap \overline{T R_2}|}{|\overline{T R_1} \cup \overline{T R_2}|}.
\]

Modified Jaccard Coefficient. Let \( t_0 \) be a TR embedded in \( Y \). Even if \( t_0 \) is a TR according to the definition, when we embed \( t_0 \) in a string \( Y \), it is well possible that \( t_0 \) is not maximal in \( Y \), thus if an algorithm reports correctly \( t' \supseteq t_0 \) there will be a slight penalization in the IC measure. This phenomenon arose a number of times, thus we decided to use a modified version of the Jaccard Coefficient, called J2C, where the denominator is changed. The resulting measure is thus more robust w.r.t. this penalization:

\[
 J_C(\overline{T R_1}, \overline{T R_2}) = \frac{|\overline{T R_1} \cap \overline{T R_2}|}{\max(|\overline{T R_1}|, |\overline{T R_2}|)}.
\]

Given a TR \( t_0 \) and a set of TRs: \( T = \{t_1, \ldots, t_s\} \) we define the best-match \( BM(t_0, T) \):

\[
 BM(t_0, T) = \arg\max_{t \in T} J_C(\overline{t_0}, \overline{t}),
\]

and the best-match-score BMS:

\[
 BMS(t_0, T) = \max_{t \in T} J_C(\overline{t_0}, \overline{t}).
\]

In our controlled experiments the evaluation module knows the embedded TR \( t_0 \) and receives the output of an algorithm \( T \), giving back the best match score. For a series of experiments we will report the average of the BMS. Note that BMS has values in the range \([0, \ldots, 1]\), and higher values correspond to better quality. At first sight one might consider this metric as overly generous. However, since we cannot rule out the existence of other TRs in \( Y \) besides the embedded ones, we do not want to penalize the presence in \( T \) of valid TRs different from \( t_0 \). Also, the set \( T \) will not contain nested TRs.

3.10 Evaluation of recall on biological sequences

The evaluation has been carried out according to the following procedure. Let \( TR_{\overline{R}}, TR_{\overline{F}}, TR_{\overline{A}} \) be the set of TRs found by TRStalker, TRF, and ATRHunter respectively. First, we removed from every set all the TRs that have a Jaccard coefficient greater than a threshold \( J \) when compared with another TR in the same set. In other words, we removed TR duplicates from every set of results, where two TRs are considered as duplicates when they cover the same region with an approximation \( J \). Since TRF and ATRHunter have been executed with options that discard all TRs having a score lower than a given threshold, we filtered \( TR_{\overline{R}} \) by removing all the TRs with a score under such value (this has been done to not penalize TRF and ATRHunter with respect to TRStalker). More in detail, TRF has been executed with match, mismatch, and indel score equal to 2, 3, and 3 respectively, maximum motif length equal to 2000bp, and threshold equal to 30.2

2 Maximum possible value for TRF.
A TRHunter has been executed with match, mismatch, gap and terminal gap score equal to 10 -10, maximum motif length equal to 500bp \(^5\) and threshold equal to 30. For the TRs found by TRStalker the score is computed by using the same weights used by TRF and ATRHunter then we filtered the results using the same threshold. After the filtering phase, we computed the union of the TRs found by all algorithms, \(U = \bigcup \{T_{TRS}, T_{TRF}, T_{ATR}\}\). The removal of duplicates with threshold \(J\) is also applied to \(U\). Naturally the higher the value of \(J\) and less filtering will be performed.

4 DISCUSSION

We have performed comparative experiments both with synthetic and with biological sequences. Here we describe the experimental set up, how the synthetic sequences are generated and the outcome of the comparison. For biological data we briefly indicate the reason why that sequence has been selected, and the new TRs found by the application of TRStalker.

4.1 Synthetic Data

4.1.1 Generation of synthetic data. We carried out a first set of experiments by using synthetic data. This allows a fine grained control on the amount of mutations introduced within the regions covered by the TRs. The sequences we gave as input to the programs have been built according to the following steps:

1. the background sequence is generated by selecting the four bases A,C,G, and T with equal probability;
2. a perfect TR is embedded within the previous sequence, the TR is generated as \(r\) repetitions of a motif with length \(l\);
3. the region covered by the TR is mutated according to substitution, insertion and deletion probabilities (\(p_s, p_i,\) and \(p_d\)); the number of substitutions, insertions and deletion for every repetition of the motif is exactly equal to \(l_p, l_i,\) and \(l_d\);
4. if the TR is a Steiner-STR, mutations are introduced in every repeat with respect to the consensus motif; if the TR is a Neighboring-TR, mutations are introduced with respect to the previous repeat.

The experiments have been carried out running ATRHunter with these parameters: match, mismatch, gap and terminal gap score equal to 10 -10 (the most permissive setting on the website); maximum motif length equal to 500bp (the maximum allowed by the tool). In order to select the definition of TRs among those allowed by ATRHunter, we performed a preliminary set of experiments: the definition that gave the best results was the third one (minimum alignment score). In this case, ATRHunter reports only the TRs that have a score higher than a given threshold. The value of the threshold has been set to 30.

For the web-based version of TRF all the experiments have been carried out with these parameters: match, mismatch, and indel score equal to 2, 3, and 5 respectively; maximum period equal to 500; minimum score equal to 30. For the binary version we used the following ones: match, mismatch, and indel score equal to 2, 3, and 3 respectively; match and indel probability equal to 0.75 and 0.20; maximum period equal to 500; minimum score equal to 30. The parameters of the experiments have been set so to make sure that the minimum allowed score for all the tools tested is attained on the input data. TRStalker is run with the error parameter \(\mu = 0.3\) and the constant \(c = 1.5\).

4.1.2 Discussion of the comparative experiments. For the experiments on Neighboring-TR (Figure 1), we tested TRs with motifs of length from 60 to 300, and a number of repeats from 2 to 8. TRStalker has recall always above 95%, TRF (binary) has always a recall above 80% except for TR with repeat number 2 for which the recall drops to 60%. ATRHunter has recall of about 60%. These experiments confirm the effectiveness of the new techniques for the initial filtering steps.

Results on Steiner-STR with motifs of length from 60 to 300, and a number of repeats from 2 to 8 are shown in Figure 2. Here we notice that all methods have degraded performance for longer motifs (above 200 bases) while TRStalker still manages to have recall above 60%. For shorter motifs (of less than 100 bases) TRF (binary) is able to match TRStalker only when the repeat number is above 6. Thus for a large range of values TRStalker attains the best performance in recall, or a matching one, always above 80%.

The time performance of TRStalker has not been yet optimized. At the moment it is within an order of magnitude of TRF and ATRHunter. More details on the running time are in the Suppl. Materials.

4.2 Biological sequences

Testing of TRStalker on biological sequences has confirmed the potential of our method for finding very fuzzy TRs not detected by TRF and ATRHunter, and, to the best of our knowledge, not reported in literature. We tested the following sequences:

1. U43748 Homo sapiens frataxin gene, promoter region and exon -2,465 bp long (FRDA).
2. L3609 Homo sapiens germline T-cell receptor beta chain, complete gene -684,973 bp long (HSBT).
3. NC_001133.8 Saccharomyces cerevisiae Chromosome I -230,208 bp long (YCh1).

4.2.1 Experimental settings. The three algorithms have been run with the setting used in the synthetic experiments\(^4\) (thus with a very permissive acceptance policy). In general, none of the three algorithms generates all TRs found by the two others, and in Table 1 we show the percentage of the TRs found by each algorithm with respect to the union of the TRs found. In Table 2 we report some very long TRs that were detected by TRStalker but missed by the other two methods. We check the motif/repeat alignments using the tool jaligner\(^5\) using the BLOSUM62 score matrix, that confirms the good quality of the motifs found (see Table 3).

4.2.2 Frederick's ataxia. Frederick's ataxia is an autosomal recessive degenerative disease involving the central and peripheral nervous system and the heart, that roughly affects 1 person in 50,000 (Wells, 2008). In 1996 it was shown (Campuzano et al., 1996) that in 98% of the cases this disease was caused by an abnormal expansion...
in the copy number of a triplet TR in the first intron of the Frataxin coding sequence. It belongs to the family of trinucleotide repeat disorders. Very recently (Vissers et al., 2009) it has been shown that the local repetitive structure of DNA may play a role in variable copy number genomic disorders. Applying TRStalker to the frataxin sequence we detected a divergent TR in positions [2036-2414], of period 188 and copy number 2, to the best of our knowledge not previously reported, that includes the breakpoint region of the repeat disorder (See Table 2). Experimental data reported in (Brodzik, 2007) on the Frataxin sequence did find a number of short TRs (of period up to 10/13) that are completely covered by the longer fuzzy TR reported by TRStalker.

4.2.3 Human Beta T cell receptor locus. The cellular immune system detects the presence of pathogens largely through the activation of T cell receptor proteins (TCR) (Ghisman et al., 2001), which come in four different families α, β, γ, and δ. The complete DNA sequence of the human β T cell receptor locus has been determined (Rowen et al., 1996) and it has been found that a large fraction of the locus sequence (about 47%) is formed by locus-specific repeats (Rowen et al., 1996). This sequence was selected as a test case for TRStalker because of its richness in repeating elements with the aim of highlighting the ability of TRStalker in finding repeats with high divergence among adjacent copies. Here (see Table 2) we could find a few such repeats apparently not recorded in the GenBank: L36092.2 record, nor found by TRF and ATRHunter (still set with very loose parameters).

4.2.4 Yeast Chromosome I. Saccharomyces cerevisiae (baker’s yeast) has been the focus of intensive study as the first eukaryotic organism whose genome was completely sequenced (Dujon, 1996), and serves as a model organism in basic genomic investigations. Chromosome I (Bussey et al., 1995) is the smallest of the 16 chromosomes present in yeast. It has been noticed that the yeast genome is remarkably poor in repeated elements (Dujon, 1996), thus finding new TRs in such organism is a challenging task for any algorithm. In Table 2 we report a TR in position [186168,188347] of copy number 2 and motif length 1089. This TR is not reported in the TRDB database, while ATRHunter in the same region finds 15 shorter TR of length ranging from 50 to 180. This region, according to the NCBI record, is rich in genes of the DUP240 gene family (encoding membrane proteins). The presence of a fuzzy repeat in this region thus suggests a possible remote gene duplication event.

4.2.5 Performance on biological sequences. Reporting interesting single new tandem repeats, as in Table 2 is useful to demonstrate that biological relevant TRs are still unknown. We give also an evaluation of the overall behavior of the three different methods on biological sequences. Thus, we compared TRStalker, TRF, and ATRHunter by estimating their recall on the three biological sequences with the methodology described in sub-section 3.10. Table 1 reports i) the number of unique TRs found by the different algorithms and ii) the percentage of the union reported by a given algorithm, with two filtering thresholds at $J = 90\%$ and $J = 70\%$. For all the three sequences, TRStalker is able to find a large number of TRs that are not discovered by using the other methods. In practice a better overall coverage can be attained by using all three methods and merging their results. Although lower $J$ values imply a more aggressive filtering, the percentage of the union attained by TRStalker is almost constant.
Table 2. Examples of TRs found by TRStalker and missed by TRF and A TRHu nter. We report the original sequence name and length, the TR starting and ending positions, the TR length and the TR repeating unit length and copy number. The score is computed by assigning +2 to matches and -1 to mismatches with respect the consensus string. The normalized score is the score divided the TR length.

<table>
<thead>
<tr>
<th>N.</th>
<th>Sequence</th>
<th>Seq. Length</th>
<th>TR Start</th>
<th>TR End</th>
<th>TR Length</th>
<th>Consensus</th>
<th>Repetitions</th>
<th>Score</th>
<th>Norm. Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>HSBT</td>
<td>684973</td>
<td>411000</td>
<td>413127</td>
<td>2127</td>
<td>1061</td>
<td>2.00</td>
<td>2868</td>
<td>1.384</td>
</tr>
<tr>
<td>2</td>
<td>HSBT</td>
<td>684973</td>
<td>448001</td>
<td>449687</td>
<td>1686</td>
<td>842</td>
<td>2.00</td>
<td>2310</td>
<td>1.370</td>
</tr>
<tr>
<td>3</td>
<td>HSBT</td>
<td>684973</td>
<td>636116</td>
<td>638622</td>
<td>2506</td>
<td>1253</td>
<td>2.00</td>
<td>3232</td>
<td>1.326</td>
</tr>
<tr>
<td>4</td>
<td>YCh1</td>
<td>232008</td>
<td>186168</td>
<td>188347</td>
<td>2179</td>
<td>1089</td>
<td>2.00</td>
<td>3053</td>
<td>1.401</td>
</tr>
<tr>
<td>5</td>
<td>FRDA</td>
<td>2465</td>
<td>2029</td>
<td>2407</td>
<td>378</td>
<td>188</td>
<td>2.011</td>
<td>501</td>
<td>1.325</td>
</tr>
</tbody>
</table>

Table 3. Motif/repeats alignment scores computed by jaligner using the BLOSUM62 score matrix with gap open penalty set to 1 and gap extend penalty set to 0.5 for the TRs reported in Table 2.

<table>
<thead>
<tr>
<th>Seq.</th>
<th>N.</th>
<th>Repeat</th>
<th>Length</th>
<th>Identity</th>
<th>Gaps</th>
<th>Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>HSBT</td>
<td>1</td>
<td>1</td>
<td>1107</td>
<td>805/1107 (72.72%)</td>
<td>91/1107 (8.22%)</td>
<td>3657.00</td>
</tr>
<tr>
<td>HSBT</td>
<td>1</td>
<td>2</td>
<td>878</td>
<td>638/878 (72.67%)</td>
<td>85/878 (9.68%)</td>
<td>3045.50</td>
</tr>
<tr>
<td>HSBT</td>
<td>2</td>
<td>1</td>
<td>878</td>
<td>638/878 (72.67%)</td>
<td>71/878 (8.06%)</td>
<td>5256.00</td>
</tr>
<tr>
<td>HSBT</td>
<td>2</td>
<td>2</td>
<td>1300</td>
<td>1000/1300 (76.92%)</td>
<td>90/1300 (7.00%)</td>
<td>5206.00</td>
</tr>
<tr>
<td>YCh1</td>
<td>4</td>
<td>1</td>
<td>1130</td>
<td>895/1130 (79.20%)</td>
<td>72/1130 (6.35%)</td>
<td>4280.50</td>
</tr>
<tr>
<td>YCh1</td>
<td>4</td>
<td>2</td>
<td>1123</td>
<td>901/1123 (79.23%)</td>
<td>72/1123 (6.46%)</td>
<td>4345.50</td>
</tr>
<tr>
<td>FRDA</td>
<td>5</td>
<td>1</td>
<td>193</td>
<td>149/193 (77.20%)</td>
<td>10/193 (5.24%)</td>
<td>723.50</td>
</tr>
<tr>
<td>FRDA</td>
<td>5</td>
<td>2</td>
<td>191</td>
<td>146/191 (76.44%)</td>
<td>15/191 (7.82%)</td>
<td>765.00</td>
</tr>
</tbody>
</table>

Table 1. Evaluation of recall for the three methods under evaluation. Each entry in the table gives the absolute number of unique TR found, and in () the percentage of unique TR w.r.t the union of the 3 methods. For TRStalker we used both a TRF-like and an ATRHunter-like filtering (more restrictive) on the TRs found.

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>filter 90%</th>
<th>filter 70%</th>
</tr>
</thead>
<tbody>
<tr>
<td>TRStalker (TRF filter)</td>
<td>59 (56.2)</td>
<td>43 (56.5)</td>
</tr>
<tr>
<td>TRStalker (ATR filter)</td>
<td>43 (41.0)</td>
<td>30 (39.4)</td>
</tr>
<tr>
<td>TRF</td>
<td>24 (22.9)</td>
<td>18 (23.6)</td>
</tr>
<tr>
<td>ATRHunter</td>
<td>24 (22.9)</td>
<td>23 (30.2)</td>
</tr>
<tr>
<td>Union</td>
<td>105 (100.0)</td>
<td>76 (100.0)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>filter 90%</th>
<th>filter 70%</th>
</tr>
</thead>
<tbody>
<tr>
<td>TRStalker (TRF filter)</td>
<td>22557 (59.1)</td>
<td>14137 (60.2)</td>
</tr>
<tr>
<td>TRStalker (ATR filter)</td>
<td>18124 (47.5)</td>
<td>11427 (48.7)</td>
</tr>
<tr>
<td>TRF</td>
<td>9977 (26.1)</td>
<td>8521 (36.0)</td>
</tr>
<tr>
<td>ATRHunter</td>
<td>7392 (19.3)</td>
<td>7034 (29.6)</td>
</tr>
<tr>
<td>Union</td>
<td>38218 (100.0)</td>
<td>23743 (100.0)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>filter 90%</th>
<th>filter 70%</th>
</tr>
</thead>
<tbody>
<tr>
<td>TRStalker (TRF filter)</td>
<td>7168 (61.8)</td>
<td>4656 (63.5)</td>
</tr>
<tr>
<td>TRStalker (ATR filter)</td>
<td>5621 (48.4)</td>
<td>3655 (49.9)</td>
</tr>
<tr>
<td>TRF</td>
<td>2892 (24.9)</td>
<td>2518 (34.1)</td>
</tr>
<tr>
<td>ATRHunter</td>
<td>2037 (17.6)</td>
<td>1958 (26.4)</td>
</tr>
<tr>
<td>Union</td>
<td>11616 (100.0)</td>
<td>7407 (100.0)</td>
</tr>
</tbody>
</table>

5 CONCLUSION

TRStalker is a novel efficient heuristic algorithm for finding Fuzzy Tandem Repeats in biological sequences. TRStalker aims at improving the capability of TR detection for a class of fuzzy TRs for which existing methods do not perform well. Initial testing on biological data show that fuzzy TRs not previously reported are present in biologically relevant sequences. In the case of the Frataxin sequence, the fuzzy TR reported is associated with the known variable copy number breakpoint of Frederich’s ataxia. Future work will involve testing TRStalker on relevant families of repetitive elements such as centromeric α-satellites. An extension of TRStalker to handle amino acid sequences is under development.

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expression. Bioinformatics, 22(6), 676-684.


